

1. $g(x) = \sqrt{5+6x}$

(a) $g'(x) = \frac{1}{2} (5+6x)^{-\frac{1}{2}} \cdot 6$
 $= 3(5+6x)^{-\frac{1}{2}} = \frac{3}{\sqrt{5+6x}}$

(b) Domain $g(x)$
 $5+6x \geq 0$
 $5+6x \geq 0$
 $6x \geq -5$
 $x \geq -\frac{5}{6}$

$= [-\frac{5}{6}, \infty)$

(c) Domain $g'(x)$
 $\sqrt{5+6x} \neq 0$ $5+6x > 0$

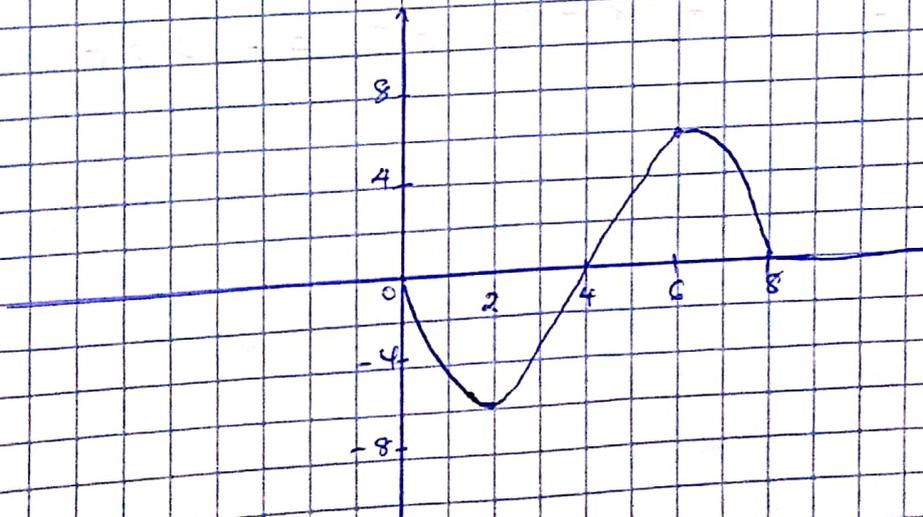
$\sqrt{5+6x} \neq 0$ $5+6x > 0$
 $5+6x \neq 0$ $6x > -5$
 $x \neq -\frac{5}{6}$ $x > -\frac{5}{6}$

$= (-\frac{5}{6}, \infty)$

2 (a) Increasing = $(2, 6)$
 Decreasing = $(0, 2) \cup (6, 8)$

(b) local maximum at $x = 6$
 local minimum at $x = 2$

(c)



$$(d) \quad f''(x) > 0 = (6, 4)$$

$$f''(x) < 0 = (4, 8)$$

$$3. \quad y = 2x^3 + 3x^2 - 12x + 9$$

$$\frac{dy}{dx} = 6x^2 + 6x - 12$$

$$6x^2 + 6x - 12 = 0$$

$$x^2 + x - 2 = 0$$

$$(x-1)(x+2) = 0$$

$$x = 1 \quad \text{or} \quad x = -2$$

$$4. \quad (a) \quad f(x) = (x-2)(x+4)$$

$$f'(x) = 1(x+4) + 1(x-2)$$

$$= x+4 + x-2 = 2x+2$$

$$(b) \quad g(x) = \frac{5x^2 - 2x + 3}{x}$$

$$g'(x) = \frac{x(10x-2) - (5x^2 - 2x + 3)}{x^2}$$

$$= \frac{10x^2 - 2x - 5x^2 + 2x - 3}{x^2} = \frac{5x^2 - 3}{x^2}$$

$$(c) \quad h(x) = x^4 - 5e^x + 2x^2$$

$$h'(x) = 4x^3 - 5e^x + 4x$$